

2020/10/26, 微積分小考 (2), §2.5 ~ §3.2 (可用鉛筆、需計算過程、交回題目卷及答案卷)

1. (5%, 15%) (a) What is the "Intermediate Value Theorem for Continuous Functions"? (b) Use the Intermediate value Theorem to prove that the equation  $x^2 + \sqrt{2x + 5} - 4 = 0$  has a solution.
2. (10%, 10%) (a) What is the definition of the derivative of a function  $f$  at a point  $x$ ? (b) What is the meaning of the function  $f$  is differentiable at  $x$ ?
3. (20%, 20%) Find the asymptotes of the graph of  $f(x)$ : (a)  $f(x) = \frac{1 - x^2}{x^2 + 1}$ . (b)  $f(x) = \frac{x^2 - 4}{x - 1}$ .
4. (20%) Show that the function  $y = |x|$  is differentiable on  $(-\infty, 0)$  and  $(0, \infty)$  but has no derivative at  $x = 0$ .

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