## 2020/05/25, 108-2 微積分小考 (2), $\S10.3 \sim \S10.8$ (可用鉛筆、需計算過程、交回題目卷及答案卷)

1. Use the Ratio Test or Root Test to determine if each series converges or diverges.

(a) 
$$\sum_{n=1}^{\infty} \frac{n!}{10^n}$$
. (b)  $\sum_{n=1}^{\infty} \frac{n \ln n}{2^n}$ .

2. Determine the convergence of the series, absolutely, conditionally or diverge?

(a) 
$$\sum_{n=2}^{\infty} (-1)^n \frac{\ln n}{n - \ln n}$$
. (b)  $\sum_{n=1}^{\infty} (-1)^n \frac{(2n)!}{2^n n! n}$ .

- 3. Find the series's radius and interval of convergence. Foe what values of x does the series converge absolutely, or conditionally? (a)  $\sum_{n=0}^{\infty} \frac{(-1)^n (x+2)^n}{n}$ . (b)  $\sum_{n=1}^{\infty} \frac{3 \cdot 5 \cdot 7 \cdots (2n+1)}{n^2 \cdot 2^n} x^{n+1}$ .
- 4. (a) Find the Maclaurin series:  $xe^x$ .
  - (b) Find the Taylor series and the Taylor polynomials generated by  $f(x) = \sin x$  at x = 0.

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