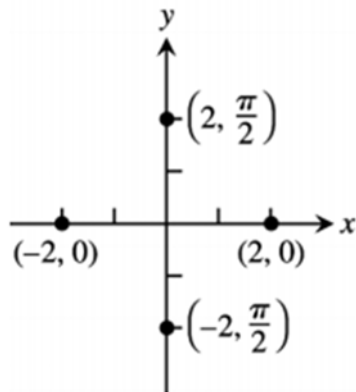
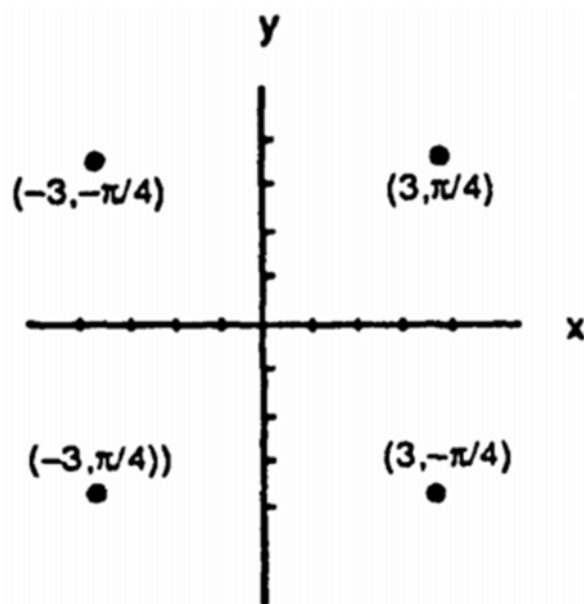


1.

(c)  $(2, \frac{3\pi}{2} + 2n\pi)$  and  $(-2, \frac{3\pi}{2} + (2n + 1)\pi)$ ,  $n$  an integer



(c)  $(3, -\frac{\pi}{4} + 2n\pi)$  and  $(-3, \frac{3\pi}{4} + 2n\pi)$ ,  $n$  an integer



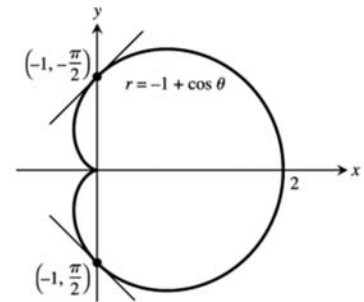
2.

38.  $r^2 \sin 2\theta = 2 \Rightarrow 2r^2 \sin \theta \cos \theta = 2 \Rightarrow (r \sin \theta)(r \cos \theta) = 1 \Rightarrow xy = 1$ , hyperbola with focal axis  $y = x$

62.  $x^2 + xy + y^2 = 1 \Rightarrow x^2 + y^2 + xy = 1 \Rightarrow r^2 + r^2 \sin \theta \cos \theta = 1 \Rightarrow r^2(1 + \sin \theta \cos \theta) = 1$

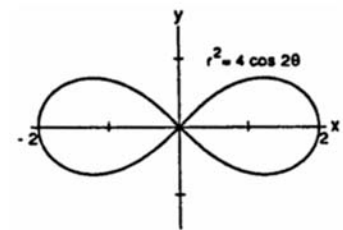
3.

$$\begin{aligned}
 17. \quad \theta = \frac{\pi}{2} &\Rightarrow r = -1 \Rightarrow \left(-1, \frac{\pi}{2}\right), \text{ and } \theta = -\frac{\pi}{2} \Rightarrow r = -1 \\
 &\Rightarrow \left(-1, -\frac{\pi}{2}\right); r' = \frac{dr}{d\theta} = -\sin \theta; \text{ Slope} = \frac{r' \sin \theta + r \cos \theta}{r' \cos \theta - r \sin \theta} \\
 &= \frac{-\sin^2 \theta + r \cos \theta}{-\sin \theta \cos \theta - r \sin \theta} \Rightarrow \text{Slope at } \left(-1, \frac{\pi}{2}\right) \text{ is} \\
 &\frac{-\sin^2\left(\frac{\pi}{2}\right) + (-1) \cos \frac{\pi}{2}}{-\sin \frac{\pi}{2} \cos \frac{\pi}{2} - (-1) \sin \frac{\pi}{2}} = -1; \text{ Slope at } \left(-1, -\frac{\pi}{2}\right) \text{ is} \\
 &\frac{-\sin^2\left(-\frac{\pi}{2}\right) + (-1) \cos\left(-\frac{\pi}{2}\right)}{-\sin\left(-\frac{\pi}{2}\right) \cos\left(-\frac{\pi}{2}\right) - (-1) \sin\left(-\frac{\pi}{2}\right)} = 1
 \end{aligned}$$



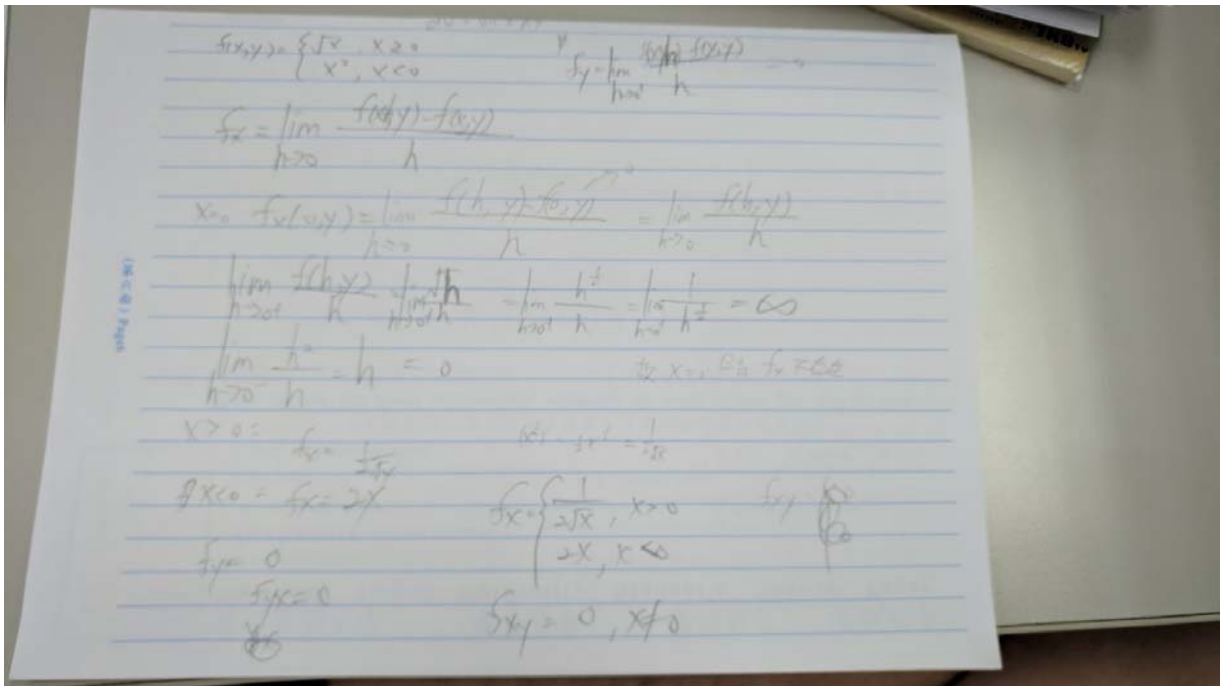
4.

13. Since  $(\pm r, -\theta)$  are on the graph when  $(r, \theta)$  is on the graph  $((\pm r)^2 = 4 \cos 2(-\theta) \Rightarrow r^2 = 4 \cos 2\theta)$ , the graph is symmetric about the x-axis and the y-axis  $\Rightarrow$  the graph is symmetric about the origin



$\theta$	$2\theta$	$\cos 2\theta$	$4 \cos 2\theta$	$\sqrt{2^2 \cos 2\theta}$
0	0°	1	4	2
$\pi/6$	30°	$1/2$	2	$\sqrt{2}$
$\pi/4$	45°	0	0	0
$\pi/3$	60°	$-1/2$	-2	-
$\pi/2$	90°	-1	-4	-

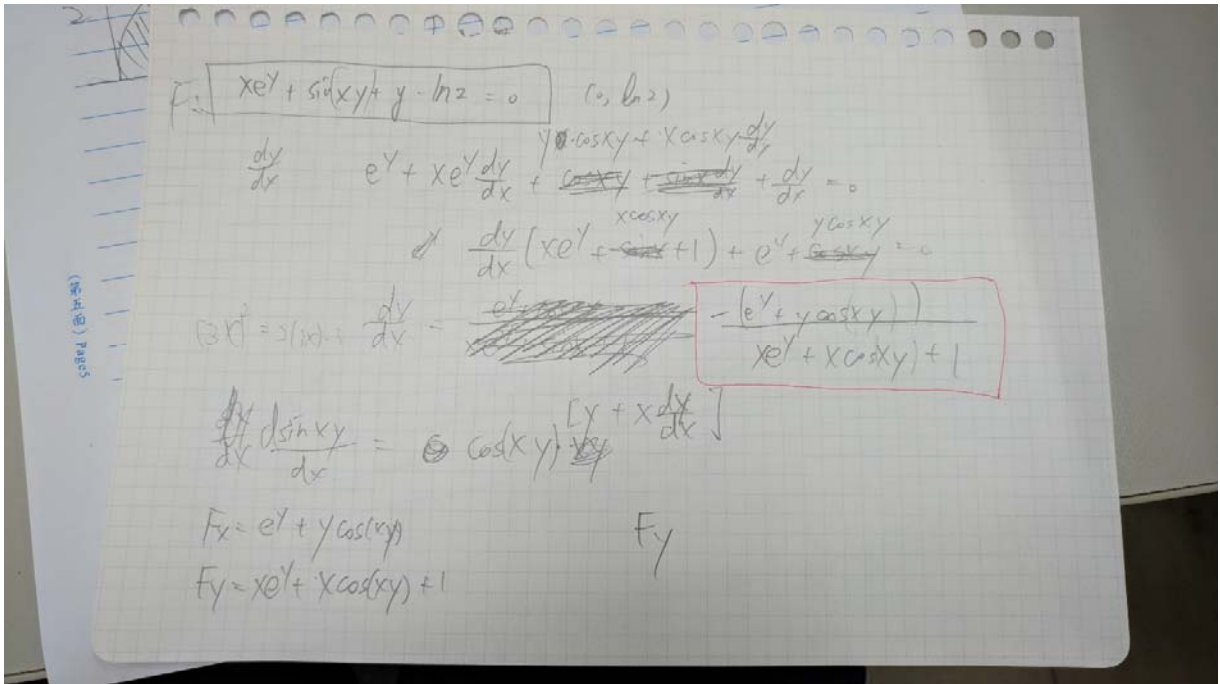
5.



6.

28. Let  $F(x, y) = xe^y + \sin xy + y - \ln 2 = 0 \Rightarrow F_x(x, y) = e^y + y \cos xy$  and  $F_y(x, y) = xe^y + x \sin xy + 1$   
 $\Rightarrow \frac{dy}{dx} = -\frac{F_x}{F_y} = -\frac{e^y + y \cos xy}{xe^y + x \sin xy + 1} \Rightarrow \frac{dy}{dx}(0, \ln 2) = -(2 + \ln 2)$

課本答案有錯



7.

After reversing the order of integration we get

$$\int_0^{1/2} \int_0^{\sin^{-1} y} xy^2 dx dy$$

Handwritten solution on a piece of paper:

$$\int_0^{\pi/6} \int_{\sin x}^{1/2} xy^2 dy dx$$

$$= \int_0^{\pi/6} x \left[ \frac{1}{3} y^3 \right]_{\sin x}^{1/2} dx$$

$$= \frac{1}{3} \int_0^{\pi/6} x \left[ \frac{1}{8} - \sin^3 x \right] dx$$

$$= \frac{1}{24} \int_0^{\pi/6} x dx - \frac{1}{3} \int_0^{\pi/6} x \sin^3 x dx$$

$$= \frac{1}{24} \left[ \frac{1}{2} x^2 \right]_0^{\pi/6} - \frac{1}{3} \left[ -x \cos x + \frac{x \cos^3 x}{3} + \sin x - \frac{1}{3} \int \cos^3 x dx \right]$$

$$= \frac{\pi^2}{48 \times 36} - \frac{1}{3} \left[ -\frac{\pi}{6} \frac{\sqrt{3}}{2} + \frac{1}{3} \times \frac{\pi}{6} \left( \frac{\sqrt{3}}{2} \right)^3 + \frac{1}{2} - \frac{1}{3} \times \frac{11}{12} \right]$$

$$= \frac{\pi^2}{1728} - \frac{1}{3} \left( -\frac{\sqrt{3}\pi}{12} + \frac{2\sqrt{3}\pi}{144} + \frac{1}{2} - \frac{11}{12} \right)$$

$$= \frac{\pi^2}{1728} - \frac{1}{3} \left( -\frac{9\sqrt{3}\pi}{144} + \frac{25}{72} \right) = \frac{\pi^2}{1728} + \frac{9\sqrt{3}\pi}{432} - \frac{25}{1728}$$

Final result:  $\frac{\pi^2}{1728} - \frac{-9\sqrt{3}\pi + 50}{432}$

Handwritten solution on a grid paper:

$$\int_0^{\pi/6} \int_{\sin(x)}^{1/2} xy^2 dy dx = \frac{\pi^2}{1728} - \frac{-9\sqrt{3}\pi + 50}{432}$$

$$\square = \int_0^{\pi/6} \cos^3 x dx = \left[ \sin x - \frac{\sin^3 x}{3} \right]$$

$$= \frac{1}{2} - \frac{\left(\frac{1}{2}\right)^3}{3} = \frac{1}{2} - \frac{1}{3} \times \frac{1}{8} = \frac{1}{2}$$

$$1 \quad \iint_R f(x, y) dA$$

To find the value of double integral, we must find the area of integration

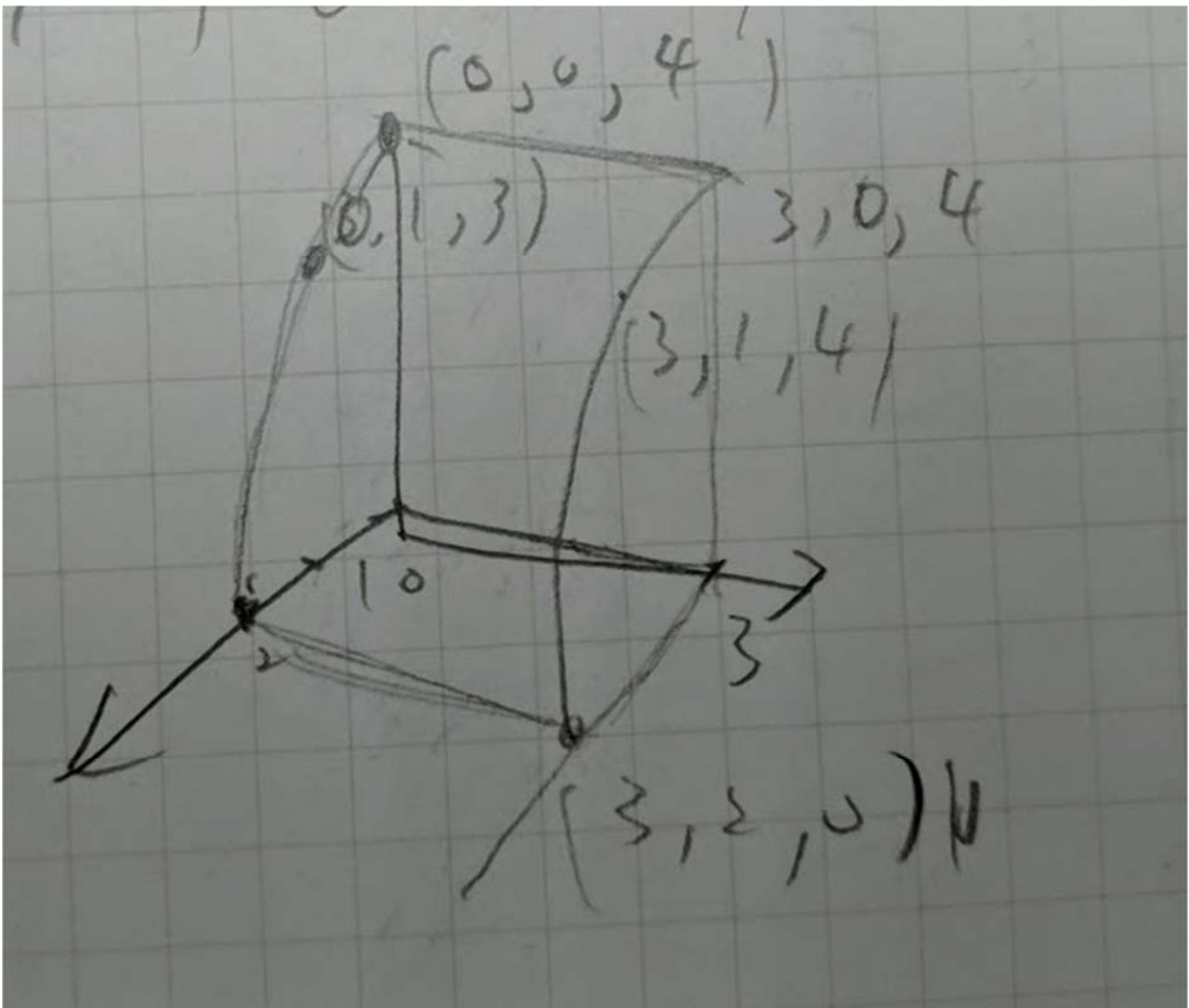
2

$$f(x, y) = 4 - y^2$$

the domain is restricted by the area  $\rightarrow x = 3$

3

$$\int_0^2 \int_0^3 (4 - y^2) dx dy = \int_0^2 [4x - y^2x]_0^3 dy = \int_0^2 (12 - 3y^2) dy = [12y - y^3]_0^2 = 24 - 8 = 16$$



9.

$$\begin{aligned}
 17. \quad & \int_{-1}^0 \int_{-2x}^{1-x} dy dx + \int_0^2 \int_{-x/2}^{1-x} dy dx \\
 &= \int_{-1}^0 (1+x) dx + \int_0^2 (1-\frac{x}{2}) dx \\
 &= \left[ x + \frac{x^2}{2} \right]_{-1}^0 + \left[ x - \frac{x^2}{4} \right]_0^2 = -(-1 + \frac{1}{2}) + (2-1) = \frac{3}{2}
 \end{aligned}$$



10.

$$\begin{aligned}
 22. \quad \text{average} &= \frac{1}{(\ln 2)^2} \int_{\ln 2}^{2 \ln 2} \int_{\ln 2}^{2 \ln 2} \frac{1}{xy} dy dx = \frac{1}{(\ln 2)^2} \int_{\ln 2}^{2 \ln 2} \left[ \frac{\ln y}{x} \right]_{\ln 2}^{2 \ln 2} dx \\
 &= \frac{1}{(\ln 2)^2} \int_{\ln 2}^{2 \ln 2} \frac{1}{x} (\ln 2 + \ln \ln 2 - \ln \ln 2) dx = \left( \frac{1}{\ln 2} \right) \int_{\ln 2}^{2 \ln 2} \frac{dx}{x} = \left( \frac{1}{\ln 2} \right) [\ln x]_{\ln 2}^{2 \ln 2} \\
 &= \left( \frac{1}{\ln 2} \right) (\ln 2 + \ln \ln 2 - \ln \ln 2) = 1
 \end{aligned}$$